

1. If x = 3 is one root of the quadratic equation  $x^2 - 2kx - 6 = 0$ , then find the value of k.

**Sol.** x = 3 is one root of the equation  $\therefore 9 - 6k - 6 = 0$  $\Rightarrow k=12 \Rightarrow k=12$ 

2. What is the HCF of smallest prime number and the smallest composite number?

**Sol.** The required number 2 and 4. HCF of 2 and 4 is 2.

- 3. Find the distance of a point P(x, y) from the origin. Sol.  $OP=x_2+y_2-\cdots-\sqrt{OP}=x_2+y_2$
- 4. In an AP, if the common difference (d) = −4, and the seventh term (a<sub>7</sub>) is 4, then find the first term.
  Sol. a + 6(-4) = 4

⇒a=28⇒a=28

- 5. What is the value of (cos² 67° − sin² 23°)?
   Sol. ∵cos67∘=sin23∘∵cos[i₀]67∘=sin[i₀]23∘
   ∴cos267∘=sin223=0∴cos267∘=sin223=0
- 6. Given ΔABC~ΔPQR,ΔABC~ΔPQR, if ABPQ=13,ABPQ=13, then find arΔABCarΔPQRarΔABCarΔPQR.
  Sol. arΔABCarΔPQR=AB2PQ2arΔABCarΔPQR=AB2PQ2 =(13)2=19=(13)2=19

# SECTION - B

7. Given that  $2-\sqrt{2}$  is irrational, prove that  $(5+32-\sqrt{})(5+32)$  is an irrational number.

**Sol.** Let us assum  $5+32-\sqrt{5}+32$  is a rational number.  $\therefore 5+32-\sqrt{=}_{pq} \therefore 5+32=pq$  where  $q\neq oq\neq o$  and p and q are integers.  $\Rightarrow 2-\sqrt{=}_{p-5q}3q \Rightarrow 2=p-5q}3q$   $\Rightarrow 2-\sqrt{\Rightarrow}2$  is a rational number as RHS is rational This contradicts the given fact that  $2-\sqrt{2}$  is rational.

Hence  $5+32-\sqrt{5+32}$  is an irrational number.



### 8. In Fig. 1, ABCD is a rectangle. Find the values of x and y.



Sol. AB = DC and BC = AD

 $\Rightarrow$ x+y=30andx-y=14} $\Rightarrow$ x+y=30andx-y=14} Solving to get x = 22 and y = 8.

9. Find the sum of first 8 multiples of 3.

**Sol.** S = 3 + 6 + 9 + 12 + ... + 24 = 3 (1 + 2 + 3 + .... + 8)

 $=3 \times 8 \times 92 = 3 \times 8 \times 92$ 

= 108

10. Find the ratio in which P(4, m) divides the line segment joining the points A(2, 3) and B(6, -3). Hence find m.

**Sol.** Let AP : PB = k : 1

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.._{6k+2k+1}=4..6k+2k+1=4
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$$\Rightarrow \Rightarrow k = 1$$
, ratio is 1:1

Hence m=-3+32=0m=-3+32=0

## 11. **Two different dice are tossed together. Find the probability:**

- i. of getting a doublet
- ii. of getting a sum 10, of the numbers on the two dice.

Sol. Total number of possible outcomes = 36

- Doublets are (1, 1) (2, 2) (3, 3) (4, 4) (5, 5) (6, 6) Total number of doublets = 6
   ∴ Prob (getting a doublet) =636=636 or 1616
- ii. Favourable outcomes are (4, 6) (5, 5) (6, 4) i.e., 3 ∴∴ Prob (getting a sum 10) =336=336 or \[112\[112



# 12. An integer is chosen at random between 1 and 100. Find the probability that it is :

- i. divisible by 8.
- ii. not divisible by 8.

**Sol.** Total number of outcomes = 98

- i. Favourable outcomes are 8, 16, 24, ..., 96 i.e., 12 ∴.. Prob (integer is divisible by 8) =1298=1298 or 649649
- ii. Prob (integer is not divisible by 8) =1-649=1-649=4349=4349

### SECTION - C

### 13. Find HCF and LCM of 404 and 96 and verify that HCF ×× LCM = Product of the two given numbers.

**Sol.**  $404=2\times2\times101=22\times101404=2\times2\times101=22\times101$  $96=2\times2\times2\times2\times2\times3=25\times396=2\times2\times2\times2\times2=23=25\times3$  $\therefore$  HCF of 404 and 96 =  $2^2$  = 4 LCM of 404 and 96 = $101\times25\times3=9696=101\times25\times3=9696$ HCF×LCM=4×9696=38784HCF×LCM=4×9696=38784 Also  $404\times96=38784404\times96=38784$ Hence HCF×LCMHCF×LCM = Product of 404 and 96.

- 14. Find all zeroes of the polynomial  $(2x^4 9x^3 + 5x^2 + 3x 1)$  if two of its zeroes are  $(2+3-\sqrt{})(2+3)$  and  $(2-3-\sqrt{})(2-3)$ . Sol. P(x) =  $2x^4 - 9x^3 + 5x^2 + 3x - 1$  $2+3-\sqrt{2}+3$  and  $2-3-\sqrt{2}-3$  are zeroes of p(x)  $\therefore$  p(x) =  $(x-2-3-\sqrt{})(x-2+3-\sqrt{})\times g(x)(x-2-3)(x-2+3)\times g(x)$ = $(x^2 - 4x + 1)g(x)$  $(2x^4 - 9x^3 + 5x^2 + 3x - 1) + (x^2 - 4x + 1) = 2x^2 - x - 1$  $\therefore$  g(x) =  $2x^2 - x - 1$ = (2x + 1)(x - 1)Therefore other zeroes are x-12x-12 and x = 1 $\therefore$  Therefore all zeroes are  $2+3-\sqrt{},2-3-\sqrt{},-122+3,2-3,-12$  and 1.
- 15. If A(-2, 1), B(a, 0), C(4, b) and D(1, 2) are the vertices of a parallelogram ABCD, find the values of a and b. Hence find the lengths of its sides.



If A(-5, 7), B(-4, -5), C(-1, -6) and D(4, 5) are the vertices of a quadrilateral, find the area of the quadrilateral ABCD.

**Sol.** ABCD is a parallelogram



 $\therefore diagonal AC and BD bisect each other$ ThereforeMid point of BD is same as mid point of AC $<math display="block"> \Rightarrow (a+12,22)=(-2+42,b+12)\Rightarrow (a+12,22)=(-2+42,b+12)$  $\Rightarrow a+12=1\Rightarrow a+12=1 and \Rightarrow b+12=1\Rightarrow b+12=1$  $\Rightarrow \Rightarrow a = 1, b = 1. Therefore length of sides are 10--10 units each.$ 

### OR

Area of quad ABCD = Ar $\Delta\Delta$ ABD + Ar $\Delta\Delta$ BCD D(4, 5) C(-1, -6) Aea of  $\Delta$ ABD=12|(-5)(-5-5)+(-4)(5-7)+(4)(7+5)| $\Delta$ ABD=12|(-5)(-5-5)+(-4)(5-7)+(4)(7+5)| = 53 sq units Area of  $\Delta$ BCD=12|(-4)(-6-5)+(-1)(5+5)+4(-5+6)| $\Delta$ BCD=12|(-4)(-6-5)+(-1)(5+5)+4(-5+6)| = 19 sq units Hence area of quad. ABCD = 53 + 19 = 72 sq units.



16. A plane left 30 minutes late than its scheduled time and in order to reach the destination 1500 km away in time, it had to increase its speed by 100 km/h from the usual speed. Find its usual speed. Sol. Let the usual speed of the plane be x km/hr ∴1500x-1500x+100=3060∴1500x-1500x+100=3060
⇒ x<sup>2</sup> + 100x - 300000 = 0
⇒ x<sup>2</sup> + 600x - 500x - 300000 = 0

$$\Rightarrow\Rightarrow (x + 600)(x - 500) = 0$$

x≠-600,x≠-600, ∴x=500∴x=500

Speed of plane = 500 km/hr

17. Prove that the area of an equilateral triangle described on one side of the square is equal to half the area of the equilateral triangle described on one of its diagonal.

### OR

If the area of two similar triangles are equal, prove that they are congruent.

Sol. Let the side of the square be 'a' units

 $\therefore AC^2 = a^2 + a^2 = 2a^2$   $\Rightarrow AC=2-\sqrt{\Rightarrow}AC=2a \text{ units}$ Area of equilateral  $\Delta BCF=3\sqrt{4}a2sq.u\Delta BCF=34a2sq.u$ Area of equilateral  $\Delta ACE=3\sqrt{4}(2-\sqrt{a})2=3\sqrt{2}a2sq.u\Delta ACE=34(2a)2=32a2sq.u$   $\Rightarrow Area\Delta BCF=12Ar\Delta ACE\Rightarrow Area\Delta BCF=12Ar\Delta ACE$ 

### OR

Let  $\triangle ABC = \triangle PQR \triangle ABC = \triangle PQR$ .

 $\therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta ABCar \Delta PQR = AB_2PQ_2 = BC_2QR_2 = AC_2PR_2 \therefore ar \Delta ABCar \Delta ABCa$ 

Given  $ar \Delta ABC = ar \Delta PQR ar \Delta ABC = ar \Delta PQR$ 

 $\Rightarrow$ AB<sub>2</sub>PQ<sub>2</sub>=1=BC<sub>2</sub>QR<sub>2</sub>=AC<sub>2</sub>PR<sub>2</sub> $\Rightarrow$ AB2PQ2=1=BC2QR2=AC2PR2

 $\Rightarrow\Rightarrow$  AB = PQ, BC = QR, AC = PR

 $\Rightarrow\Rightarrow$  Therefore  $\triangle ABC \cong \triangle PQR \triangle ABC \cong \triangle PQR$  (sss congruence rule)



18. Prove that the lengths of tangents drawn from an external point to a circle are equal.



To prove PT=QT Proof: Consider the triangle OPT and OQT. OP=OQ  $\angle OPT=\angle OQT=90^{\circ}$  OT=OT (common side) Hence by RHS the triangles are equal. Hence PT = QT Hence Proved.

19. If  $4\tan\theta=3,4\tan[f_0]\theta=3$ , evaluate  $(4\sin\theta-\cos\theta+14\sin\theta+\cos\theta-1)(4\sin[f_0]\theta-\cos[f_0]\theta+14\sin[f_0]\theta+\cos[f_0]\theta-1)$ 

### OR

If tan 2A = cot (A – 18°), where 2A is an acute angle, find the value of A.

Sol.  $4\tan\theta = 34\tan[i_0]\theta = 3$   $\Rightarrow \tan\theta = 34 \Rightarrow \tan[i_0]\theta = 34$   $\Rightarrow \sin\theta = 35 \Rightarrow \sin[i_0]\theta = 35$  and  $\cos\theta = 45\cos[i_0]\theta = 45$   $\therefore 4\sin\theta - \cos\theta + 14\sin\theta + \cos\theta - 1 = 4 \times 35 - 45 + 14 \times 35 + 45 - 1$   $= 4 \times 35 - 45 + 14 \times 35 + 45 - 1$ = 1311 = 1311

#### OR

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tan2A = cot(A - 18^{\circ})

\Rightarrow \Rightarrow 90^{\circ} - 2A = A - 18^{\circ}

\Rightarrow \Rightarrow 3A = 108^{\circ}

\Rightarrow \Rightarrow A = 36^{\circ}
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20. Find the area of the shaded region in Fig. 2, where arcs drawn with centres A, B, C and D intersect in pairs at mid-points P, Q, R and S of the sides AB, BC, CD and DA respectively of a square ABCD of side 12 cm. [Use  $\pi\pi$  = 3.14].



Sol. Radius of each are drawn = 6cm Area of one quadrant = $(3.14)\times_{364}=(3.14)\times_{364}$ Area of four ABCD = $3.14\times_{36}=113.04$ cm2= $3.14\times_{36}=113.04$ cm2 Area of square ABCD x= $12\times_{12}=144$ cm2x= $12\times_{12}=144$ cm2 Hence Area of shaded region = 144 - 113.04= 30.96 cm<sup>2</sup>

21. A wooden article was made by scooping out a hemisphere from each end of a solid cylinder, as shown in Fig. 3. If the height of the cylinder is 10 cm and its base is of radius 3.5 cm. Find the total surface area of the article.



Fig. 3

OR

A heap of rice is in the form of a cone of base diameter 24 m and height 3.5 m. Find the volume of the rice. How much canvas cloth is required to just cover the heap?

**Sol.** Total surface Area of article = CSA of cylinder + CSA of 2 hemispheres

CSA of cylinder  $2\pi rh2\pi rh$ 

=2×227×3.5×10=2×227×3.5×10

= 220 cm<sup>2</sup>



Surface Area of two hemispherica scoops  $=4 \times 227 \times 3.5 \times 3.5 = 4 \times 227 \times 3.5 \times 3.5 = 154$  cm<sup>2</sup> Total surface Area of article = 220 + 154 = 374 cm<sup>2</sup>

OR

Radius of conical heap = 12m Volume of rice = $13 \times 227 \times 12 \times 12 \times 3.5 \text{ m}^3 = 13 \times 227 \times 12 \times 12 \times 3.5 \text{ m}^3 = 528 \text{ m}^3$ Area of canvas cloth required = $\pi \text{rl}=\pi \text{rl}$   $l=122+(3.5)2-----\sqrt{=12.5 \text{ml}=122+(3.5)2=12.5 \text{m}}$   $\therefore$  Area of canvas required = $227 \times 12 \times 12.5 = 227 \times 12 \times 12.5$ = 471.4 m<sup>2</sup>

### 22. The table below shows the salaries of 280 persons:

Salary (In thousand Rs)	No. of persons
5 - 10	49
10 - 15	133
15 - 20	63
20 - 25	15
25 - 30	6
30 - 35	7
35 - 40	4
40 - 45	2
45 - 50	1

### Calculate the median salary of the data. Sol.

Salary (In thousand Rs)	No. of persons	cf
5 - 10	49	49
10 - 15	133	182
15 - 20	63	245
20 - 25	15	260
25 - 30	6	266
30 - 35	7	273
35 - 40	4	277
40 - 45	2	279
45 - 50	1	280



N2=2802=140N2=2802=140 Median class is 10-15 zMedian =l+hf(N2-C)=l+hf(N2-C)=10+5133(140-49)=10+5133(140-49) =10+5×91133=10+5×91133 = 13.42 Median salary is Rs 13.42 thousand or Rs 13420 (approx)

### SECTION - D

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23. A motor boat whose speed is 18 km/
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hr in still water takes 1hr more to go 24 km upstream than to return

downstream to the same spot. Find the speed of the stream.

OR

A train travels at a certain average speed for a distance of 63 km and then travels at a distance of 72 km at an average speed of 6 km/hr more than its original speed. If it takes 3 hours to complete total journey, what is the original average speed?

**Sol.** Let the speed of stream be x km/hr.

 $\label{eq:linear} $$:The speed of the boat upstream = (18-x)km/hr and speed of the boat downstream = (18+x)km/hr} \\ $$:The speed of the boat upstream = (18-x)km/hr and speed of the boat upstream = (18-x)km/hr} \\ $$:The speed of the boat upstream = (18-x)km/hr$ 

As given in the question,

2418 - x - 2418 + x = 12418 - x - 2418 + x = 1

 $\Rightarrow x^2 + 48x - 324 = 0$ 

 $\Rightarrow\Rightarrow (x + 54)(x - 6) = 0$ 

x≠−54, x≠−54, ∴∴ x = 6

 $\therefore$  speed of the stream = 6km/hr.

### OR

Let the original average speed of train be x km/hr. Therefore  $_{63x+72x+6}=363x+72x+6=3$  $\Rightarrow\Rightarrow x^2 - 39x - 126 = 0$  $\Rightarrow\Rightarrow (x - 42) (x + 3) = 0$ 



 $x \neq -3x \neq -3$  ∴x = 42∴x = 42Original speed of train is 42 km/hr.

# 24. The sum of four consecutive numbers in an AP is 32 and the ratio of the product of the first and the last term to the product of two middle terms is 7 : 15. Find the numbers.

```
Sol. Let the four consecutive terms of the A.P. be

a - 3d, a - d, a + d, a + 3d.

By given conditions

(a - 3d) + (a - d) + (a + d) + (a + 3d) = 32

\Rightarrow \Rightarrow 4a = 32

\Rightarrow \Rightarrow a = 8

and (a-3d)(a+3d)(a-d)(a+d)=715(a-3d)(a+3d)(a-d)(a+d)=715

\Rightarrow \Rightarrow 8a^2 = 128d^2

\Rightarrow \Rightarrow d^2 = 4

\Rightarrow \Rightarrow d=\pm 2d=\pm 2

\therefore Number are 2, 6, 10, 14 or 14, 10, 6, 2.
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25. In an equilateral ΔABC,ΔABC, D is a point on side BC such that BD=13BCBD=13BC. Prove that 9(AD)<sup>2</sup> = 7(AB)<sup>2</sup>

### OR

Prove that, in a right triangle, the square on the hypotenuse is equal to the sum of the squares on the other two sides.

Sol. Draw AELBCAELBC  $\Delta \Delta AEB \cong \Delta AEC\Delta AEC$  (RHS congruence rule)  $\therefore BE=EC=12BC=12AB \therefore BE=EC=12BC=12AB$ Let AB = BC = AC = x Now BE=x2BE=x2 and DE = BE - BD =x2=x3=x2=x3 =x6=x6NowAB2=AE2+BE2....(1)andAD2=AE2+DE2.....(2)}NowAB2=AE2+BE2....(1) andAD2=AE2+DE2.....(2)}



From (1) and (2)  $AB^2 - AD^2 = BE^2 - DE^2$   $\Rightarrow x_2 - AD_2 = (x_2)_2 - (x_6)_2 \Rightarrow x_2 - AD_2 = (x_2)_2 - (x_6)_2$  $\Rightarrow AD_2 = x_2 - x_2 + x_2 + x_2 - x_2 + x_2 + x_2 - x_2 + x_2 +$ 

#### OR

**Given:** A right triangle,  $\triangle \triangle ABC$  right angled at B. To prove:  $AC^2 = AB^2 + BC^2$ 

**Construction:** Draw  $AD \perp ACAD \perp AC$ .

We need to use the following theorem to prove the above result: Theorem 1: If a perpendicular is drawn from the vertex of a right angle of a right triangle to the hypotenuse, then triangles on each side of the perpendicular are similar to each other and to the whole triangle. The figure is shown below:



Using the theorem 1 stated above, we get  $\Delta ABD \sim \Delta ACB \Delta ABD \sim \Delta ACB$ Since the corresponding sides of similar triangles are proportional, we

have

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ADAB=ABACADAB=ABAC
```

Cross multiply to get,

 $AB^2 = AC \times AD \dots (1)$ 

Again, using the theorem 1 stated above, we get

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\Delta BDC \sim \Delta ABC \Delta BDC \sim \Delta ABC
```

Since the corresponding sides of similar triangles are proportion, we have

```
\begin{array}{l} & \text{BCAC=DCBCBCAC=DCBC} \\ & \text{Corss multiply to get,} \\ & \text{BC2=AC\times DCBC2=AC\times DC ..... (2)} \\ & \text{Add (1) and (2) to get,} \\ & \text{AB2+BC2=AC\times AD+AC\times DCAB2+BC2=AC\times AD+AC\times DC} \\ & =\text{AC}\times(\text{AD+DC})=\text{AC}\times(\text{AD+DC}) \end{array}
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=AC×AC=AC×AC = AC<sup>2</sup> Thus it is proved that,  $AB^2 + BC^2 = AC^2$ 

# 26. Draw a triangle ABC with BC = 6 cm, AB = 5 cm and $\angle \angle ABC = 60^{\circ}$ . Then construct a triangle whose sides are 3434 of the corresponding sides of the $\triangle ABC \triangle ABC$ .

**Sol.** A  $\Delta A'BC'\Delta A'BC'$  whose sides are 3434 of the corresponding sides  $\Delta ABC\Delta ABC$  can be drawn as follows.

## step 1

draw a  $\triangle ABC \triangle ABC$  with side BC = 6cm, AB = 5cm

and  $\angle ABC = 60 \circ \angle ABC = 60 \circ$ .

## step 2

Draw a ray BX making an acute angle with BC on the opposite side of vertex A.

## step 3

Locate 4 points (as 4 is greater in 3 and 4),  $B_1$ ,  $B_2$ ,  $B_3$ ,  $B_4$ , on line segment BX.

# step 4

Join  $B_4C$  and draw a line through  $B_3$ , parallel to  $B_4C$  intersecting BC at C'. step 5

Draw a line through C' parallel to AC intersecting AB at A'.  $\Delta A'BC'\Delta A'BC'$  is the required triangle.



## Justification

The construction can be justified by proving  $A'B=_{34}AB, BC'=_{34}BC, A'C'=_{34}ACA'B=_{34}AB, BC'=_{34}BC, A'C'=_{34}ACA'B=_{34}AB, BC'=_{34}BC, A'C'=_{34}ACB'=_$ 



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 \angle A'BC' = \angle ABC \angle A'BC' = \angle ABC \text{ (Common)} \\ \therefore \Delta A'BC' \sim \Delta ABC \therefore \Delta A'BC' \sim \Delta ABC \text{ (A similarity criterion)} \\ \Rightarrow A'BAB = BC'BC = AC'AC \Rightarrow A'BAB = BC'BC = A'C'AC \dots (1) \\ In \Delta BB_3C' \Delta BB_3C' and \Delta BB_4C, \Delta BB_4C, \\ \angle B_3BC' = \angle B4BC \angle B3BC' = \angle B4BC \text{ (Common)} \\ \angle BB_3C' = \angle BB_4C \angle BB_3C' = \angle BB_4C \text{ (Corresponding angles)} \\ \Rightarrow BC'BC = BB_3BB_4 \Rightarrow BC'BC = BB_3BB_4 \\ \Rightarrow BC'BC = 34 \Rightarrow BC'BC = 34 \dots (2) \\ From equations (1) and (2), we obtain \\ A'BAB = BC'BC = A'C'AC = 34A'BAB = BC'BC = A'C'AC = 34 \\ \Rightarrow A'B = 34AB, BC' = 34BC, A'C' = 34AC \Rightarrow A'B = 34AB, BC' = 34BC, A'C' = 34AC \\ This justifies the construction.
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# 27. **Prove that**

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: sinA-2sin_3A2cos_3A-cos_A=tanAsin_{fo}A-2sin_3A2cos_3A-cos_{fo}A=tan_{fo}A

Sol. LHS =sinA-2sin_3A2cos_3A-cos_A=sin_{fo}A-2sin_3A2cos_3A-cos_{fo}A

=sinA(1-2sin_2A)cos_A(2cos_2A-1)=sin_{fo}A(1-2sin_2A)cos_{fo}A(2cos_2A-1)

=sinA(1-2(1-cos_2A))cos_A(2cos_2A-1)=sin_{fo}A(1-2(1-cos_2A))cos_{fo}A(2cos_2A-1)

=tanA(2cos_2A-1)(2cos_2A-1)=tan_{fo}A(2cos_2A-1)(2cos_2A-1)

= tanA = RHS
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# 28. The diameters of the lower and upper ends of a bucket in the form of a frustum of a cone are 10 cm and 30 cm respectively. If its height is 24 cm, find :

- i. The area of the metal sheet used to make the bucket.
- ii. Why we should avoid the bucket made by ordinary plastic ? [Use  $\pi\pi = 3.14$ ]

**Sol.** Here  $r_1 = 15$  cm,  $r_2 = 5$  cm and h = 24 cm

(i) Area of metal sheet = CSA of the bucket + area of lower end = $\pi l(r_1+r_2)+\pi r_{22}=\pi l(r_1+r_2)+\pi r_{22}$ 

where  $l=242+(15-5)2-----\sqrt{26}$  cml=242+(15-5)2=26 cml=242+(15-5)2=26

 $\therefore$  Surface area of metal

sheet = $3.14(26 \times 20 + 25)$ cm2= $3.14(26 \times 20 + 25)$ cm2

= 1711.3cm<sup>2</sup>

(ii) we should avoid use of plastic because it is non-degradable or **similar value**.

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29. As observed from the top of a 100 m high light house from the sea-level, the angles of depression of two ships are 30° and 45°. If one ship is exactly behind the other on the same side of the light house, find the distance between the two ships. [Use 3-\sqrt{3} = 1.732] Sol. Let AB be the tower and ships are at points C and D.
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# 30. The mean of the following distribution is 18. Find the frequency f of the class 19 – 21.

Class	11-13	13-15	15-17	17-19	19-21	21-23	23-25
Frequency	3	6	9	13	f	5	4

### OR

The following distribution gives the daily income of 50 workers of a factory :

Daily Income (in Rs) 🛛 🦷	100-120	120-140	140-160	160-180	180-200
Numbers of workers	12	14	8	6	10

Convert the distribution above to a less than type cumulative frequency distribution and draw its ogive.

Sol.

Class	X	f	fx
11-13	12	3	36
13-15	14	6	84
15-17	16	9	144
17-19	18	13	234
19-21	20	f	20f
21-23	22	5	110
23-25	24	4	96
		40 + f	704 + 20f



Mean =18=704+20f40+f=18=704+20f40+f  $\Rightarrow 720 + 18f = 704 + 20f$  $\Rightarrow f = 8$ 

### OR

Cumulative frequency distribution table of less than type is

Daily income	Cumulative frequency	
Less than 100	0	
Less than 120	12	
Less than 140	26	
Less than 160	34	
Less than 180	40	
Less than 200	50	

